## ÇANKAYA UNIVERSITY Faculty of Arts and Sciences <br> Course Definition Form

Part I. Basic Course Information


| Course Name <br> This information will appear in the printed catalogs and on the web online catalog. <br> English <br> Name | Algebra |
| :--- | :--- |
| Turkish | Cebir |

## Course Description

Provide a brief overview of what is covered during the semester. This information will appear in the printed catalogs and on the web online catalog Maximum 60 words.
Groups, Subgroups, Lagrange's Theorem, Normal Subgroups, Quotient Groups, Homomorphisms, Direct Products, Semidirect Products, Group Action on Sets, Cayley's Theorem, The Class Equation, Sylow Theorems, Rings, Fields, Integral Domains, Prime Ideals, Maximal Ideals, Rings of Polynomials, Factorization of Polynomials over a Field, Homomorphisms, Factor Rings, Unique Factorization Domains, Euclidean Domains, Field Extensions, Algebraic Extensions, Finite Fields.


## Part II. Detailed Course Information

## Course Objectives

Maximum 100 words
The aim of the course is to give the necessary background about theory of groups, rings and fields.

## Learning Outcomes

Explain the learning outcomes of the course. Maximum 10 items.
The students will learn:

1. definitions of a group, a ring, an integral domain, a field and some basic examples.
2. how to construct a quotient group.
3. how to construct a quotient ring.
4. how to determine a given ideal is prime or maximal.
5. how to determine isomorphisms between groups or rings.
6. how to factorize of a given polynomial over a field and determine irreducible polynomials.
7. to determine Unique Factorization Domains, Euclidean Domains.
8. how to construct extension of fields.

| Textbook(s) <br> List the textbook(s), if any, and other related main course material. |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Author(s) | Title | Publisher | Publication <br> Year | ISBN |
| Thomas W. <br> Hungerford | Abstract Algebra, An Introduction, Third <br> Edition | Brooks/Cole, <br> Cengage <br> Learning | 2014 | ISBN-13: <br> $978-1-I n-56962-4 ~$ |


| Reference Books <br> List, if any, other reference books to be used as supplementary material. |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Author(s) | Title | Publisher | Publication <br> Year | ISBN |
| Michael Artin | Algebra | Pearson | 2010 | ISBN-13: <br> $978-0132413770 ~$ |
| Joseph J. Rotman | A First Course in Abstract Algebra with <br> Applications | Pearson | 2005 | ISBN-13: <br> $978-0131862678 ~$ |
| David S. Dummit, <br> Richard M. Foote | Abstract Algebra | Wiley | 2003 | ISBN-13: <br> $978-0471433347 ~$ |
| John B. Fraleigh | A First Course in Abstract Algebra | Pearson | 2002 | ISBN-13: <br> $978-0201763904$ |
| D. S. Malik, John M. <br> Mordeson, M. K. Sen | Fundamentals of Abstract Algebra | Mcgraw-Hill | 1996 | ISBN-13: <br> $978-0070400351 ~$ |

## Teaching Policy

Explain how you will organize the course (lectures, laboratories, tutorials, studio work, seminars, etc.)
4 hours of lecturing per week. Attendance to the lectures is compulsory.

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Computer Usage
Briefly describe the computer usage and the hardware/software requirements for the course
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| Course Outline <br> List the weekly topics to be covered. |  |
| :---: | :--- |
| Week | Topic(s) |
| 1 | Groups, Cyclic Groups, Dihedral Groups, Permutation and Symmetry Groups |
| 2 | Subgroups, Cosets, Lagrange's Theorem, Normal Subgroups |
| 3 | Quotient Groups, Group homomorphisms, Isomorphisms |
| 4 | Direct Products, Semidirect Products, Finitely Generated Abelian Groups |
| 5 | Group Action on Sets, Cayley's Theorem, The Class Equation |
| 6 | Sylow Theorems |
| 7 | Rings, Ideals, Quotient Rings, Ring Homomorphisms |
| 8 | Ring Isomorphisms, Prime and Maximal Ideals |
| 9 | Integral Domains, Euclidean Domains |
| 10 | Principle Ideal Domains, Unique Factorization Domains |
| 11 | Polynomials |
| 12 | Field Extensions, Algebraic Elements, Transcendental Elements |
| 13 | Finite Extensions, Algebraically Closed Fields |
| 14 | Finite Fields |


| Grading Policy |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| List the assessment tools and their percentages that may give an idea about their relative importance to the end-of-semester grade. |  |  |  |  |  |  |  |  |
| Assessment Tool | Quantity | Percentage | Assessment Tool | Quantity | Percentage | Assessment Tool | Quantity | Percentage |
| Homework |  |  | Case Study |  |  | Attendance |  |  |
| Quiz(es) |  |  | Lab Work |  |  | Field Study |  |  |
| Midterm Exam | 2 | 60 | Classroom <br> Participation |  |  |  |  |  |
| Term Paper |  |  | Oral <br> Presentation |  |  | Final Exam | 1 | 40 |


| ECTS Workload <br> List all the activities considered under the ECTS. |  |  |  |
| :---: | :---: | :---: | :---: |
| Activity | Quantity | Duration (hours) | Total Workload (hours) |
| Attending Lectures (weekly basis) | 14 | 2 | 28 |
| Attending Labs/Recitations (weekly basis) | 14 | 2 | 28 |
| Compilation and finalization of course/lecture notes (weekly basis) | 14 | 1 | 14 |
| Collection and selection of relevant material (once) | 1 | 8 | 8 |
| Self study of relevant material (weekly basis) | 14 | 2 | 28 |
| Take-home assignments |  |  |  |
| Preparation for quizzes |  |  |  |
| Preparation for mid-term exams (including the duration of the exams) | 2 | 14 | 28 |
| Preparation of term paper/case-study report (including oral presentation) |  |  |  |
| Preparation of term project/field study report (including oral presentation) |  |  |  |
| Preparation for final exam (including the duration of the exam) | 1 | 16 | 16 |
| TOTAL WORKLOAD / 25 |  |  | 150/25 |
| ECTS Credit |  |  | 6 |

Total Workloads are calculated automatically by formulas. To update all the formulas in the document first press CTRL+A and then press F9.

Program Qualifications vs. Learning Outcomes Consider the program qualifications given below as determined in terms of learning outcomes and acquisition of capabilities for all the courses in the curriculum. Look at the learning outcomes of this course given above. Relate these two using the Likert Scale by marking with $X$ in one of the five choices at the right.

| No | Program Qualifications | Contribution |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No |  | 0 | 1 | 2 | 3 | 4 |
| 1 | Adequate knowledge in mathematics; ability to use applied and theoretical information in these areas to solve pure and applied mathematics problems. |  |  |  |  | X |
| 2 | Ability to use modern computational tools to analyze an abstract or real life problem |  |  |  | X |  |
| 3 | Adequate knowledge in theoretical and historical background in mathematics |  |  |  | X |  |
| 4 | Ability to work individually and in teams efficiently, ability to collaborate effectively in teams to analyze complex systems from intra-disciplinary and multi-disciplinary areas |  |  |  | X |  |
| 5 | Ability to communicate effectively in English about technical subjects, both orally and in writing |  |  |  | X |  |
| 6 | Ability to use, develop and implement new experiments and algorithms to solve scientific, engineering and financial problems |  |  |  | X |  |
| 7 | Ability to analyze a mathematical problem using both analytical and numerical methods; use and compare theoretical and simulational methods to gain deeper insight |  |  |  | X |  |
| 8 | Ability to report the findings, conclusions and interpretations related to a project in the area of pure and applied mathematics, ability to write technical reports, to prepare and conduct effective presentations |  |  |  | X |  |
| 9 | Recognition of the need for lifelong learning; ability to access information, to follow developments in science and technology, and to keep continuous self improvement |  |  |  | X |  |
| 10 | Awareness of professional and ethical responsibility issues and their legal consequences |  |  |  |  | X |

Scale for contribution to a qualification: 0-none, 1-little, 2-moderate, 3-considerable, 4-highest


[^0]:    Laboratory/Studio Work
    Give the number of laboratory/studio hours required per week, if any, to do supervised laboratory/studio work and list the names of the laboratories/studios in which these sessions will be conducted.

